

pxxy means

page xx

y = t top of page

y = m middle of page

y = b bottom of page

In equations "a" sometimes looks like a truncated "d".

A p13b p73m p116t,p285b area of sail, usually in  $m^2$ , often normal to Sol, p58T.

p35b area normal to energy propagation

p93b area of solar thruster

A p88b component of cyclic pitch

p119b aphelion in fig.4.7.

**a** p39m sail acceleration

**a** p174m,p198t radiation pressure acceleration, eq.5.2a, eq.5.65a.

au p13b astronomical unit 149.598E9 m

$a_0$  p14t,p58t,p134m characteristic acceleration of a sail at one au.

$a_0 = 2\eta P/\sigma$ . See also  $\kappa$ .

p39b note that  $\alpha = 0$ .  $a_0 = (9.12\eta/\sigma)$  mm/s<sup>2</sup> if  $\sigma$  is in g/m<sup>2</sup>

p40t Add to text:  $a_0 = 9.12/\sigma^* = 5.961 \beta\eta$

$a_0$  p162t Initial value of semi-major axis a.

a p47b absorption coefficient

a p67t hole size of perforated film.

a p119b,122t,153t semi-major axis fig.4.7, 1/2 dist P to A.  $a = (r_A+r_P)/2$ .

$\Delta a$  p1.53m,p1.55m,p1.58t,p160b Change in semi-major axis a per orbit.

a p195m aphelion of Keplerian orbit, not displaced circular orbit.

a p272b acceleration.

$\tilde{a}$  p273m thermally limited acceleration.

$a_\rho, a_z$  p208t accelerations in  $\rho$  and  $z$  directions?

**B** p36m magnetic field

B p88b component of cyclic pitch

$B_f$  p48m non-Lambertian reflection coefficient, front of sail.

$B_b$  p48b non-Lambertian reflection coefficient, back of sail.

b p67t size of film between holes of perforated sail

C p35t,p84m chord width of heliogyro blade

C p113b center of mass of Sol-sail system.

$C_1, C_2, C_3, C_4$  pp205m,206m,202b,206b for definitions. The dashed lines in figs.5.14-5.16.

c p35t,p83b speed of light

$c_1, c_2, c_3$  p53m parameters for billowing sail

c p67t not sure hwy this is in diagram.

D p75m total length of spars for polygonal sail

$D_c$  p73m circumference of disc sail with radius R

$D_i$  p167b  $i = 1,2,3,4$  constants of motion.

$D_s$  p73m totl length of four diagonal spars for square sail

D p273b Fresnal zone lens diameter.

d p36b take differential

p81t distance of control vane from origin, fig. 3.13.

d p273b sail diameter.

$d_i$  p81t vane location relative to center of mass, including payload

$d_s$  p273b laser beam spot diameter.

E p35t Energy

p122t,p157m Energy per unit mass.

E p279m laser energy (per unit mass?).

E p286b Kinetic energy of impinging particle, usually hydrogen.

$E'$  p279m laser energy in moving system.

$\tilde{E}$  p2286b Kinetic energy of impinging particle after passing thru sail.

**E** p36m electric field

$E_i$  p167b  $i = 1,2,3,4$  constants of motion.

**E#** my usage for 10<sup>#</sup>  
**E<sub>R</sub>** p274m Energy expended by rocket.  
**e** p42t base of natural logs.  
**e** p119b,125b eccentricity in fig.4.7. For conic  $(x/a)^2 + (y/b)^2 = 1$   
 $e = c/a = -1 + r_p v_p^2 / \mu$ , etc.  $e = (r_A - r_P) / (r_A + r_P)$ .  
**e<sub>1</sub>, e<sub>2</sub>, e<sub>3</sub>** p77b Unit vectors for fig. 3.13. **e<sub>3</sub>** = -**n**  
**F(r;t)** p42m energy flux  
**F(r)** p45m deviation of pressure of an extended source from P\*,  
the point source pressure.  $F(r) = P(r) / P^*(r)$   
**F<sub>1</sub>, F<sub>2</sub>** p167 assorted functions.  
**f** p36m, p38b, force  
**f<sub>a</sub>** p47m from absorption (same as **f<sub>i</sub>** p36m)  
**f<sub>e</sub>** p47m force from emission by re-radiation.  
**f<sub>i</sub>** p36m force from incident light,  
**f<sub>r</sub>** p36m, 47m force from reflected light  
p47m forces: ,  
p78m force on sail along **n**  
p117 net force on perfect sail fig.4.4.  
**f<sub>rs</sub>** p48m force in direction **s**, fig.2.7.  
**f<sub>ru</sub>** p48m force in direction **n**, fig.2.7.  
**f<sub>n</sub>** p49b force in direction **n**, fig.2.7.  
**f<sub>t</sub>** p49b force in direction **t**, transverse to **n**, fig.2.7.  
**f<sub>0</sub>** p53b force for billowing sail normal to Solar radius.  $\theta = 0$ .  
**f** p137t force vector, while *f* is true anomaly.  
*f* p119b true anomaly fig4.7, etc.  
*f* p152b,p162t Fig..4.26. Angle around Terra from down-Sol line to sail.  
*f* p279t light pressure force.  
*f*( $\alpha$ ) p133m part of eq.4.49.  
*f<sub>0</sub>* p162t Initial angle of *f* p.157 fig.4.30.  
*f<sub>1</sub> f<sub>2</sub> f<sub>i</sub> f<sub>r</sub>* p93t various forces for photon thruster  
 $\odot f_s$  p78m force on sail perpendicular to Sol  
*f<sub>r</sub>* p84b radial centripetal force density of heliogyro blade  
*f<sub>v</sub>* p81t force on vane when it is perpendicular to Sol  
*f<sub>x</sub>* p84b chordwise centripetal force density of heliogyro blade  
*f<sub>q</sub>* p116t force in arbitrary direction *q*.  
*f<sub>λ</sub>* p137m force component in direction  $\lambda$ .  
**G** p40t Newton's constant  $G = 6.6726 \text{ E-11 m}^3 / (\text{s}^2 \text{kg})$ . see  $\mu$ .  
**g** p17b Terra's standard gravity, 9.81 m/s<sup>2</sup>.  
**g** p14m,p39m grams  
**g<sub>i</sub>** p209b gain coefficients.  
**gI<sub>SP</sub>** p248t May be same as exhaust velocity.  
**H** p148b Hamiltonian, non-standard  
p66b Hamiltonian, standard,  $H \equiv T + V$ .  
**h** p35t Planck's constant  
**h** p83b thickness of heliogyro blade  
p121b orbital angular momentum per unit mass.  
**I** p86b moment of inertia of heliogyro blade in cross section.  
 $I = C^3 h / 12$   
**I** p113b Inertial reference frame. See fig. 4.1.  
**I'** p114m Inertial reference frame at C fig 4.1.  
**I<sub>sp</sub>** p17,p248t specific impulse of rocket. Change in momentum divided  
by change in weight on Terra, or  $\Delta m v / \Delta m g$ . Measured in seconds.  
Sloppy. Better use is change in momentum divided by change in  
mass, units of (exhaust) velocity.  
**I<sub>v</sub>(r,u;t)** p40b specific intensity of light  
**I<sub>0</sub>** p44m frequency integrated specific intensity.  $I_0 = L_S / 4\pi^2 R_S^2$   
**I<sub>C</sub>** p74t moment of inertia of disc sail circumference sail boom  
**I<sub>S</sub>** p74t moment of inertia of square sail booms  
**IR** p67t infra-red  
**i** p119b inclination of orbit WRT ecliptic plane fig.4.7.  
**i** p221b root(-1)  
**J** p36m Joules  
**j** p36m electric current

**K** p62t degrees Kelvin  
**K** p207b control matrix, used for both pitch and area. Confusing.  
**k** p42t Boltzman's constant  
**k** p202b defines an axis for skewed (my word) Type III planetary orbit.  
 kg kilograms  
**L** p73m side of square sail  
 $L_S$  p35b Solar luminosity  
**l** or script **l** p67t IR antenna length. This should be made consistent.  
**l** p151m unit vector from Sol when **r** is referenced from planet.  
 p197b same as above. Note that it is almost parallel to z-axis.  
 $\Delta l$  p37m thickness  
 script **l** p77b length of articulating boom. Is "articulating" the proper word?  
**M** p78b torque on perfect sail with off center payload  
 p79t components  $M_x M_y M_z$  of **M**  
**M** p113b mass of Sol  
 $M_S$  p40t mass of Sol 1.989 E30 kg  
**M<sub>i</sub>** p81t control torque  
 $M_x M_y M_z$  components of **M<sub>i</sub>**  
 $M_0$  p88m torque to twist root of heliogyro blade  
**M** p120m mean anomaly  $M = n(t-\tau)$   
**M** Chapter 5. Assorted matrices, not sure.  
**m** p49b unit vector in direction of total force, fig. 2.7.  
**m** p14b,p36m meters  
**m** p14t, p113b mass of sail, structure, and payload in kg.  
 p58t  $m = m_s + m_p$  total mass (sail+structure)+payload  
**m dot** p274m propellant mass flow.  
 $m_0$  p35t rest mass of a body.  
 $m_0$  p274m initial mass of rocket.  
 $m_1$  p17b mass at time one.  
 $m_2$  p17b mass at time two.  
 $m_f$  p174m final mass of rocket.  
 $m_H$  p286t rest mass of hydrogen.  
 $m_p$  p58t p77m mass of sail payload  
 $m_p$  p54t mass of proton  
 $m_s$  p58t p78m mass of sail and support structure  
**mm** p14m,p39b millimeters  
**N** p13b,p36t,p61b Newtons  
**N** p41m number of photons  
**N,N'** p119b ascending and descending nodes fig. 4.7.  
**N** p74b number of spars of length R on polygonal sail  
**n** p38b,p151m,p174m(fig.5.1),p197b unit vector normal to sail  
 p79b unit vector normal to control vanes, specifically  
 p93t unit vector along line of net force  
**n<sub>1</sub>, n<sub>2</sub>** p79b fig. 3.13 normals to tip vanes  
**n** p120m mean motion  $n = \sqrt{\mu/a^3}$ .  
**n dot** p286t rate hydrogen atoms hit sail. Which reference frame?  
**n** p225b number density of hydrogen atoms in sail frame of reference.  
 $n_0$  p225b number density of hydrogen atoms in interstellar space.  
**O** p44m Big Oh, order of magnitude  
**P** p13b,p58t Pressure of sunlight. At one au  $P = 4.56 \text{ E-6 N/m}^2$   
 p36t double for reflecting surface  $P = 9.12 \text{ E-6 N/m}^2$   
 p36t p90m Pressure on a surface  
 p94m p116t solar radiation pressure  
**P** p119b perihelion in fig.4.7.  
**P** p272b Laser output power.  
**P** p286m back pressure on sail from impacting hydrogen atoms.  
**P'** p279m Laser power as seen in moving frame.  
**P(r;t)** p42b radiation pressure tensor  
**P(r)** p43b radiation from an extended uniformly bright source  
**P\*(r)** p44b radiation pressure from a point source, or a distant  
 extended source.  $P^*(r) = L_S/2\pi r^2$   
 $P_w$  p54t Pressure of solar wind  $= 3\text{E-9 N/m}^2 = P$   
 $P_n$  p85m photon pressure normal to heliogyro blade

**$P, P_{ij}$**  p192 Matrix and components, not understood.  
 **$\bar{O}P$**  p273m Maximum laser power.  
 **$p$**  p35t,p41b momentum  $\mathbf{p} = (hv/c)\mathbf{u}$  for photons  
 **$\mathbf{p}^\wedge$**  p115t reference direction perpendicular to orbital plane.  
 **$p$**  p35t momentum  
 p119m semi-latus rectum,  $p = a(1-e^2)$ . ( $p=r$  if  $e=0$ )  
 **$p_\xi, p_\eta, p_\theta$**  p166m conjugate momenta  
 **$\mathbf{p}_r$**  p148b co-state for position  
 **$\mathbf{p}_v$**  p148b co-state for velocity, aka primer vector, optimum direction  
 of sail force vector. Huh?  
 **$Q$  dot** p286t energy flux. Per unit mass?  
 **$\mathbf{q}$**  p115m unit vector along which to maximize force.  
 **$\mathbf{R}$**  p113b position vector to center of mass of Sol-sail fig. 4.1.  
 **$R$**  p18t payload mass fraction  $R = (m_2/m_1)$   
 **$R$**  p73m p90m radius of disc sail  
 **$R$**  p74b length of spar on polygonal sail  
 **$R$**  p83b blade length of heliogyro  
 p124b and following.  $R = 1$  au., confusing notation. Use  $R_T$  or  $R_C$ .  
 **$R$**  p175t ratio of rocket energy to light sail energy.  
 **$R_E$**  p35b,p49m,p63m Sol-Terra distance  $\equiv 1$  au. I use  $r_T$ . 149.598E9 m  
  
 **$R_S$**  p44t Solar radius  
 **$R_T$**   
 **$R_i$**  p248t mass ratios.  
 **$r$**  p35b,p63m distance from Sol  
 **$r$**  p84b distance along heliogyro blade  
 **$r$**  p125b aphelion of transfer orbit, and radius of target circular orbit.  
 Confusing, better would be  $r_A$ .  
 p90m radial distance on a disc sail.  
 p118t radial distance from Sol.  
 p119b radial distance from Sol fig.4.7.  
 **$r$**  p165b distance from Sol, here distance of planet from sol. Question :  
 $r = \sqrt{(x^2 + y^2 + z^2)} = (\xi^2 + \eta^2)/2$  ?  
 **$r$**  p173b distance from Sol, fig.5.1.  
 **$r_A$**  p125b I would use this instead of  $r$  for aphelion of transfer orbit.  
 **$r_0$**  p131t radius of original circular orbit.  
 p199b Orbit chosen for its period,  $r_0 = 30 r_{\text{planet}}$  p199b.  
 **$\mathbf{r}$**  p113b vector from Sol to sail fig. 4.1.  
 **$\mathbf{r}$**  p151m vector from Terra to sail fig. 4.1.  
 **$\mathbf{r}^\wedge$**  p39b unit vector radial from Sol, often =  $\mathbf{u}_i$ .  $^\wedge$  should be atop  $\mathbf{r}$ .  
 p113b unit vector from Sol to sail fig. 4.1.  
 **$\tilde{r}$**  p47b,p63m,p272b  $r$  tilda. reflection coefficient  $r$ .  
 **$\mathbf{r}_p$**  p77b payload position vector on movable boom  
 **$\mathbf{r}_c$**  p78m Center of mass position vector of sail with moveable payload.  
 **$\mathbf{r}_1, \mathbf{r}_2$**  p113b position vectors of Sol and sail in fig. 4.1.  
 **$\tilde{r}$**  p225t reflection co-efficient.  
 **$\mathbf{S}$**  p78m Sol line vector, usually called  $\mathbf{u}$ .  
 **$S$**  p120m radial force per unit mass.  
 p166b Hamilton-Jacobi function. Oh, sure.  
 p274t distance from laser (and  $\sim$  lens) to sail.  
 **$S(\rho, z)$**  p177b limiting surface for Type I orbits.  
 **$s$**  p14b,p36m seconds  
 **$s$**  p48m another specular reflection coefficient, those into direction  $\mathbf{s}$ .  
 **$\mathbf{s}$**  p47b unit vector of specularly reflected light.  
 **$s$**  p128m linear distance  
 **$s$**  p173b distance to interstellar sail.  
 **$\tilde{S}$**  p274t maximum sail distance for full laser acceleration.  
 **$s_0$**  p276m initial distance where laser acceleration starts.  
 **$T$**  p18m mission duration  
 p42t black body temperature of sol  
 p48b,p63m sail temperature  
 p90m radial tension in a disc sail film, including rotation. N/m  
 p120m,p153m transverse (tangential) force per unit mass.

p122t, 173m, 175b orbital period  
 p134mb Transfer time in days  
 p165b kinetic energy per unit mass  
 $T$  p199t Orbital period,  $T = 2\pi/\omega$ .  
 $T$  p273m Sail equilibrium temperature.  
 $T^-$  p163b Transverse acceleration averaged over one orbit.  
 $\check{T}$  p273m Maximum allowed sail temperature.  
 $T_0$  p90m tension on rim of disc sail from membrane, not counting centripetal force. N/m of rim  
 $T_S$  p126m Half orbit transit time for solar sail.  
 $T_H$  p126m Half orbit transit time for Hohmann orbit.  
 $T_1$  p212b Curve, fig.5.22.  
 $T_2$  p213b Curve, fig.5.22.  
 $t, \Delta t$  p35b, 120m time  
 $\check{t}$  p278t time needed to reach diffraction limit.  
 $\mathbf{t}$  p47b unit vector normal to  $\mathbf{n}$ .  
 $t_\theta$  p86b twisting moment of heliogyro blade from photon pressure.  
 $t_0$  p133m time at start of logarithmic orbit.  
 UV p61b ultra-violet  
 $U$  p37m energy density  
 $U$  p174b, p198m modified potential  $U \equiv V + \Phi$ .  
 $\mathbf{u}$  p40b p47b unit vector in direction of Sol's light  
 $\mathbf{u}_f$  p39b unit vector of reflected light  
 $\mathbf{u}_i$  p39b p93t unit vector of incident light, often  $\mathbf{r}^\wedge$ , or  $\mathbf{u}$   
 $\mathbf{u}_r$  p38b p93t unit vector of reflected light  
 $u$  p274m rocket exhaust speed.  
 $V$  p165b potential energy per unit mass. Note  $\kappa$ , extra.  
 $V$  p174m, p198t potential energy per unit mass for standard gravity field.  
 Eqs.5.2b, 2.24., eq.5.65b.  
 $-\Delta V$  p174m gravitational acceleration.  
 $\Delta v$  p17b change in velocity  
 $v$  p17, p122t, p128m velocity  
 $v(r)$  p131b velocity of solar sail.  
 $v_w$  p54 velocity of solar wind = 700 km/s  
 $v_r$  p131b radial velocity of solar sail.  
 $v_\theta$  p131m transverse velocity of solar sail.  
 $v_E$  p131m circular speed of Terra.  
 $v_M$  p131m circular speed of Mars.  
 $v_0$  p131m Speed of sail at start of logarithmic orbit, Terra to Mars.  
 p276m Speed of sail where laser acceleration starts.  
 $v_\infty$  p276b Terminal speed of light sail.  
 $v_{-f}$  p131m Speed of sail at end of logarithmic orbit, Terra to Mars.  
 $v^H$  p279t velocity four vector. ?  
 $\Delta v_S$  p126b Impulse needed to go from Hohmann to circular orbit.  
 $\Delta v_H$  p126b Total impulse needed from circular to circular orbit via Hohmann transfer.  
 $\Delta v$  p126b generalized total impulse for changing circular orbits.  
 $\Delta v_1$  p134m, p136t Impulse to go from Terra circular to logarithmic spiral.  
 $\Delta v_2$  p134m, p136t Impulse to go from logarithmic spiral to Mars circular.  
 $\Delta v_T$  p134m Total of  $\Delta v_1$  and  $\Delta v_2$ .  
 $W$  p35b energy flux. p49m solar flux  
 p120m orbit normal force per unit mass.  
 $W_E$  p35b p63m (Solar) energy flux at 1 AU  
 p36m = 1368 J/s/m<sup>2</sup>  
 $w$  p85m vertical deflection of heliogyro blade Confuses with p86b  
 $w$  p86b  $w \equiv \theta x$ , not italic theta Confuses with p85m. Or perhaps these are the same if  $w$  is a function of both  $x$  (chord) and  $r$  (distance from root).  
 p90m displacement of a disc sail out of its plane  
 $x$  p84b distance across chord from centerline of heliogyro blade  
 $x_j$  p209m components of state vector  
 $x, y, z$  p36b Cartesian co-ordinates, left handed per fig. 2.1  
 p77b Cartesian co-ordinates, right handed per fig. 3.1.3, for

ideal square sail. Corresponding unit vectors are  $\mathbf{e}_1, \mathbf{e}_2, \mathbf{e}_3$ .  
p165b, Cartesian co-ordinates, with z aligned to sail normal.

z p173m axial cylinder co-ordinate.

° degree symbol

<> p36b time averaged quantity

∂ P36b partial derivative

• p38b dot product cosine included angle

✕ p36m cross product not correct symbol sine included angle

∫ p42m integral

√ square root

≡ definition

≈ p114b approximately equal

♦ p118b Used as symbol for Aries.

p122m The curved arrowhead is just the regular "less than".

<> p246m averaging symbol

Problems: cross product,  $\mathbf{r}^{\wedge}$  and  $r \cdot$ . Aries symbol. For tilde above use character code 06E4 followed by the character under the tilde.

Need formulae for del notation in various co-ordinate systems.

In cylindrical co-ordinates,  $\text{del} \equiv \rho^{\wedge}(\partial/\partial\rho) + \theta^{\wedge}(1/\rho)(\partial/\partial\theta) + \mathbf{z}^{\wedge}(\partial/\partial z)$ . Note also that  $\partial\rho/\partial\theta = \theta^{\wedge}$  and  $\partial\theta/\partial\rho = -\mathbf{r}^{\wedge}$ . All other partials = 0. And  $\rho^{\wedge}\times\mathbf{z}^{\wedge} = -\theta^{\wedge}$ ,  $\theta^{\wedge}\times\mathbf{z}^{\wedge} = \rho^{\wedge}$ ,  $\rho^{\wedge}\times\theta^{\wedge} = \mathbf{z}^{\wedge}$ .

▽ ariel Unicode ms down triangle ∽ ∽

CLCB p69b p76m Continuous Longeron Coilable Boom

DLC p26m,p65m Diamond Like Carbon

IAE p71m Inflatable Antenna Experiment

JPL p71b Jet Propulsion Lab

Lambertian p48m equally bright from any aspect.

LHS notes Left Hand Side

MEMS p97b MicroElectroMechanical Systems

RHS notes Right Hand Side

STEM p69m p70t Storable Tubular Expandable Member

Type I: fixed orbital period (fixed  $\omega$ ) for all radii  $r$  and projections onto the solar plane  $\rho$ . p177

Type II: Period at  $r$  is same as Keplerian period at  $\rho$ , so that  $\omega = \tilde{\omega}$ .

Type III: Minimum solar sail lightness number  $\beta$ . Period derives from this, depending on  $z$  and  $\rho$ .

Ellipse relationships

$a$  = semi-major axis,  $b$  = semi-minor axis,  $f$  = true anomaly,  $e$  = eccentricity

$A$  = aphelion,  $P$  = perihelion,  $r$  = radius,  $v$  = speed,  $P$  = period

$\gamma$  = flight angle (McInnes version),  $\mu = (M+m)G$  = gravitational parameter

$a^2 = b^2 + c^2$   $e = c/a$

$r = [a(1-e^2)]/(1 + e(\cos f))$   $r_p = a(1-e)$   $r_A = a(1+e)$   $2a = r_A + r_p$

$(x/a)^2 + (y/b)^2 = 1$   $x = c + r(\cos f)$   $y = r(\sin f)$

$r_1 v_1(\cos f_1) = r_2 v_2(\cos f_2) = r_A v_A = r_P v_P$   $P^2 = (4\pi^2/\mu)a^3$ ,

$v^2(r) = \mu[2/r - 1/a]$   $v^2(r_p) = 2\mu r_A/[r_p(r_A + r_p)]$   $v^2(r_A) = 2\mu r_p/[r_A(r_A + r_p)]$

$v^2(r_{\text{circular}}) = (\mu/r)$   $v^2(r_{\text{parabolic}}) = \mu(2/r)$

$(\cos \gamma)^2 = [1 + e(\cos f)]^2/[1 + e(\cos f) + e^2] = a^2(1 + e^2)/[r(2a - r)]$

Maximum of  $(\cos \gamma)$  is  $\sqrt{[1 - e^2]}$  and occurs at  $(\cos f) = -e = -c/a$ , at  $r = a$ , or at  $(x, y) = (0, \pm b)$ .

Put in index: pitch angle  $\alpha$ , cone angle  $\theta$  p49b p115. see

ΑΒΓΔΕΖΗΘΙΚΑΜΝΞΟΠΡΣΤΥΦΧΨΩ αβγδεζηθικλμνξοπρςστυφχψω ϑ script theta

$\alpha$  p15mb,p39m,p63m sail pitch angle Fig. 1.12 Angle between sun line and sail normal. Same as resulting force direction if  $\eta = 1$ .  
p78t here in x-z plane

p93t angle between sol line (or sail axis?) and net force  $\mathbf{n}$

p115t Cone angle  $\alpha$  is between  $\mathbf{n}$  and  $\mathbf{r}$ .

$\alpha$  p173m,p197b sail pitch angle

$\tilde{\alpha}$  p115m cone angle for arbitrary direction  $\mathbf{q}$

p137m angle from sun line to  $\boldsymbol{\lambda}$ , desired direction of force.

$\alpha^*$  p116m, 138t optimum sail cone angle maximizing force in desired direction  $\mathbf{q}$ .

$\alpha^*$  p133m optimum sail pitch angle (cone angle?) minimizing logarithmic transfer time.

$\alpha^*$  p133m p157b Optimum sail pitch angle.

$\beta$  p40t,p113b,p118b sail loading parameter.  $\beta = (\text{local radiation pressure acceleration})/(\text{local solar gravitation acceleration})$ . AKA lightness number of solar sail.

$\beta$  p173m sail lightness number.  $\beta = 1$  (hovers) if  $\sigma = \sigma^* = 1.53 \text{ g/m}^2$ .

$\beta$  p215m  $\beta = (\text{local radiation pressure force})/(\text{local solar gravitation force})$ , equivalent to above.

$\beta$  p279m  $\beta \equiv v/c = \text{speed as fraction of lightspeed}$ .

$\Gamma$  p198m scalar potential for solar radiation. Eq.5.67a.

$\gamma$  p130m angle between sail velocity and circular velocity.

p137b&139m angle between sail velocity and transverse direction.

$\gamma$  p174t fig.5.1. Not sure of definition. Sail elevation angle p.180b? See eq.5.56 p193m,  $\alpha = \gamma \text{atan}(z/\rho)$ .

$\gamma$  p279t Lorentz relativistic factor.  $\gamma \equiv 1/\sqrt{1-\beta^2}$ ,  $\beta \equiv v/c$ .

$\Delta$  p17 change or increment.

$\nabla$  del notation.

$\delta$  p79b rotation angle of  $\mathbf{n}_1$  and  $\mathbf{n}_2$ , perpendicular to x-axis with  $\delta = 0$  when they are parallel to  $\mathbf{n}$ . Rotation is clockwise when seen from origin.

p115t Clock angle  $\delta$  is rotation of  $\mathbf{n}$  about  $\mathbf{r}$  measured from reference  $\mathbf{p}^\wedge$  perpendicular to orbit plane

$\tilde{\delta}$  p115m Clock angle for arbitrary direction  $\mathbf{q}$ .

$\delta$  p137m Clock angle for required force direction  $\boldsymbol{\lambda}$ .

$\delta^*$  p138t optimal clock angle to maximize force in desired direction.

$\delta$  p180b perturbation

$\delta\mathbf{n}, \delta\gamma$  p189m small changes in  $\mathbf{n}$  and  $\gamma$ .

$\delta\alpha, \delta\kappa$  p207b small changes in sail pitch angle  $\alpha$  and acceleration  $\kappa$ .

$\epsilon$  p48bp273m surface emissivity

$\epsilon_b$  p48b,p63m surface emissivity, back of sail

$\epsilon_f$  p48b,p63m surface emissivity, front of sail

$\epsilon_0$  p36b permittivity of free space

$\zeta$  p223b small displacement along z-axis.

$\eta$  p14t,39b,58t sail efficiency, may be albedo

p164b second parabolic co-ordinate.

p223b small displacement along y-axis.

non-italic theta

$\theta$  p43b,p44t angle fig.2.5

$\theta_0$  p43b angular radius of Sol italic  $\theta$

p49b cone angle between incoming light and net force, fig. 2.7.

p77b position angle of  $m_p$  in fig. 3.13, boom elevation angle

$\theta$  p86b blade twist  $w \equiv \theta x$ . Not italic. Again, a slope not angle, unless you assume the small angle tangent approximation.

p118t azimuth co-ordinate from Aries  $\blacklozenge$  .

p154t reference angle, also f

p164b third parabolic co-ordinate.

$\theta$  p174t rotation angle fig.5.1.

p197b rotation angle in fig.5.13, probably WRT x-axis.

p273b diffraction limited divergence angle of laser.

$\theta_0$  p88m blade twist (aka slope) of heliogyro blade at root. Not italic  $\theta$

$\theta(t)$  p88b twist (slope) of heliogyro blade at root including collective pitch  $\theta_0$  and cyclic pitch

$\theta_0$  p88b collective pitch of heliogyro blade

special italic theta  $\vartheta$  for italic theta, special symbols font.

$\vartheta$  p85m coning angle, actual a slope.  $\vartheta = dw/dr$  Italic theta.

$\iota$  iota not used

$\kappa$  p151m,p162m,198t magnitude of solar sail acceleration,  $= a_0$  at one au.

$\kappa_0$  p202m fixed value for sail acceleration for graphing.

$\Lambda_1$  p59b  $\Lambda_2$   $\Lambda_3$  sensitivity constants

$\lambda_{IR}$  p67t Infra-red wavelength

$\lambda$  p44t aspect angle.  $\lambda = \pi/2 - \theta + \theta_0$ , see sec. 2.5.3.

$\lambda_{light}$  p67t wavelength of visible light

$\lambda$  p74t mass of spar per unit length. Note: this should not be a constant considering the forces involved change with size.

$\lambda$  p273b laser wavelength.

$\lambda(Z)$  p137t  $\lambda(Z) = (\lambda_1, \lambda_2, \lambda_3)$  function of sail orbit elements from p120t.

$\lambda_1$   $\lambda_2$   $\lambda_3$  are the coefficients of **S,T,W** from p120t. I think.

$\mu$  p114b,p118b  $\mu = G(M+m)$  per unit mass?

$\mu$  p151m  $\mu = G(M+m)$  here  $M$  is mass of Terra.

$\mu = GM_S = 1.327 \text{ E}20 \text{ m}^3/\text{s}^2$ ,  $\mu = GM_T = 3.986 \text{ E}14 \text{ m}^3/\text{s}^2$ .

$\mu\text{m}$  p14t micrometers

$\mu_0$  p36b permeability of free space

$\tilde{\mu}$  p121b effective gravitational parameter,  $\tilde{\mu} = \mu(1-\beta)$ .

$\mu$  p214b,p216b  $\mu \equiv m_2/(m_1+m_2)$ ,  $m_1$  the luminous body. For Sol-Terra,  $\mu = 3.036\text{E}-6$ .

$\nu$  p35t photon frequency

$\xi$  p43m  $\xi \equiv \cos\theta$

p164b first parabolic co-ordinate.

p223b small displacement along x-axis

$\xi_E$  p286t fraction of hydrogen atom kinetic energy transferred to sail.

$\xi_P$  p286m efficiency of momentum transfer from impinging hydrogen atoms.

$\omicron$  omicron not used.

$\pi$  p40m,p73m pi 3.14159...

$\rho$  p54 proton number density for high solar wind at 1 au =  $4\text{E}6/\text{m}^3$

$\rho$  p84b density of heliogyro blade sail film.

p211 real coefficient of  $i$

$\rho$  p173m radius of orbit displaced distance  $z$  from gravitational center along orbital axis.  $\rho$  is radius from Sol projected onto plane containing Sol.

$\sigma$  p14t p39m,p56t,p90m,p175m solar sail mass per unit area  $\sigma = m/A$ .

p221m real component of  $s$ .

$\sigma_0$  p88m radial stress/unit volume at heliogyro blade root from eq. 3.26a

$\sigma_r$  p84b radial tensile stress/unit volume in heliogyro blade

$\sigma_s$  p58t sail assembly loading: mass of sail and structure per unit area.  $\sigma_s = m_s/A$

$\sigma_x$  p84b chordwise tensile stress/unit volume in heliogyro blade

$\sigma^*$  p40m critical solar loading parameter.  $\sigma^* = L_S/2\pi GM_S c = 1.53 \text{ g}/\text{m}^2$ , sail can hover  $\beta = 1$ .

$\tilde{\sigma}$  p48b,p63m,p273m Stephan-Boltzman constant.  $5.67\text{E}-8 \text{ W}/\text{m}^2\text{K}^4$

$\tau$  p47b transmission coefficient, 0 since sail is opaque

$\tau$  p120t time of perihelion passage

p167b time-like variable.

$\tau_0$  p167b constant of motion.

$\tau$  p279t proper relativistic time.

$\tau_0$  p280m Time constant.  $\tau_0 \equiv m_0 c^2/2P$ .

$\upsilon$

$\Phi$  p174b,p198m scalar potential eq.5.3a and eq.5.66a.

p212t subtends off-solar axis Orbit I in fig.5.21.

$\varphi$  p43b angle

p50m centerline angle between force vector and sail normal, fig.2.7.  $\tan\varphi = f_t/f_n$

p77b position angle of  $m_b$  fig. 3.13, boom azimuth angle from x-axis

p118t altitude angle

p203b Fig.5.17 Angle twixt radius from Sol and axis of off-(solar) axis Type III orbit.

p212t Fig.5.21 Angle twixt radius from Sol and axis of off-(solar) axis Type III orbit.

$\chi$  p182b eq.5.24e.  
 $\Psi_{\nu}(\mathbf{r}, \mathbf{u}; t)$  p41b photon distribution  
 $\psi_{\nu}(\mathbf{r}, \mathbf{u}; t)$  p41m photon number density.  $\psi_{\nu} = (2/h^3)(e^{h\nu/kT}-1)$  for black body.  
 $\psi_0$  p88b phase angle of cyclic pitch of heliogyro blade. Measured  
in radians?  
 $\psi$  p157t Angle sun line **l** to sail velocity **v**.  
 $\Omega$  p40b solid angle p43b  $d\Omega = \sin\theta d\theta d\phi$   
p119b longitude of ascending WRT Aries. node fig. 4.7.  
 $\Omega$  p83b angular velocity of heliogyro radians/s for equations, often  
rpm in graphs.  
p90m angular velocity of disc sail  
 $\omega$  p119b angle between ascending node *N* and perihelion *P* fig.4.7.  
 $\omega$  p174t.p197b angular velocity fig.5.1, fig.5.13.  
 $\omega$  p175b,p199t angular speed  $\omega \equiv 2\pi/T$ .  
 $\tilde{\omega}$  p175b Orbital circular velocity for Keplerian orbit with radius *r*.  
p199m Same as above, maybe.  
 $\omega_s$  p223t angular rate synodic lunar month